Name	Reg. No	Class

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4E/5N

ADDITIONAL MATHEMATICS 4049/02

PAPER 2 [90 marks]

PRELIMINARY EXAMINATION

23 August 2024

2 hours 15 minutes

Candidates answer in the Question Paper
No additional material required

INSTRUCTIONS TO CANDIDATES

Do not open this booklet until you are told to do so.

Write your name, register number and class on all the work you hand in.

Write in dark blue or black pen.

You may use a pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer **ALL** questions.

You are reminded of the need for clear presentation in your answers.

Write the brand and model of your calculator in the space provided below.

INFORMATION FOR CANDIDATES

You are expected to use an electronic calculator to evaluate explicit numerical expressions.

If the degree of accuracy is not specified in the question, and if the answer is not exact, the answer should be given to **three** significant figures. Answers in degrees should be given to **one** decimal place.

For π, use either your calculator value or 3.142, unless the question requires the answer in terms of π.

The number of marks is given in brackets [ ] at the end of each question or part question.

The total of the marks for this paper is **90**.

Brand / Model of Calculator	*For Examiner's Use*

This question paper consists of **17** printed pages, including **1** blank page.

Setter: Mr Tan Boon Yong Vetter: Mr Nara

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Mathematical Formulae

1. ALGEBRA

Quadratic Equation

For the equation $ax^2 + bx + c = 0$,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Binomial expansion

$$(a+b)^n = a^n + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^2 + \ldots + \binom{n}{r}a^{n-r}b^r + \ldots + b^n,$$

where n is a positive integer and $\binom{n}{r} = \frac{n!}{(n-r)!r!} = \frac{n(n-1)\ldots(n-r+1)}{r!}$.

2. TRIGONOMETRY

Identities

$$\sin^2 A + \cos^2 A = 1$$

$$\sec^2 A = 1 + \tan^2 A$$

$$\operatorname{cosec}^2 A = 1 + \cot^2 A$$

$$\sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$$

$$\cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$$

$$\tan(A \pm B) = \frac{\tan A \pm \tan B}{1 \mp \tan A \tan B}$$

$$\sin 2A = 2 \sin A \cos A$$

$$\cos 2A = \cos^2 A - \sin^2 A = 2\cos^2 A - 1 = 1 - 2\sin^2 A$$

$$\tan 2A = \frac{2\tan A}{1 - \tan^2 A}$$

Formulae for ΔABC

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$\text{Area of } \Delta = \frac{1}{2}ab \sin C$$

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1 **(a)** Find the remainder when $3x^3 - x^2 + 4x + 2$ is divided by $x^2 + 1$. [2]

(b) The remainder when $x^3 + ax$, where a is a constant, is divided by $x + 2$ is the same as the remainder when it is divided by $x - 1$. Find the value of a. [3]

2 The area and width of a rectangle is $\left(19 - 3\sqrt{5}\right)$ cm^2 and $\left(2 + 2\sqrt{5}\right)$ cm respectively. Express the length of the rectangle in the form of $\left(a\sqrt{5} + b\right)$ cm where a and b are rational numbers. [5]

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3 **(i)** Find the term independent of x and the $\frac{1}{x^3}$ term in the binomial expansion of $\left(x^2 - \frac{2}{x}\right)^9$. [4]

(ii) Hence, find the term independent of x in the expansion of $\left(3 - x^3\right)\left(x^2 - \frac{2}{x}\right)^9$. [2]

[Turn Over

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4 Given that $\sin A = -\frac{3}{5}$ and $\cos B = -\frac{8}{17}$, where angle A and angle B are in the same quadrant, find the **exact values** of

(i) $\tan(A+B)$ [3]

(ii) $\cos\frac{B}{2}$ [3]

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5 **(a)** A curve has the equation $y = \dfrac{2x-3}{3x+4}$, where $x \neq -\dfrac{4}{3}$.

The normal to the point P on the curve where $x > 0$, is parallel to the line $y = -\dfrac{25}{17}x + 2$. Find the coordinates of P. [4]

(b) Show the function $y = \dfrac{4}{3}x^3 - x^2 + 3x - 10$ is always increasing for all real values of x. [3]

[Turn Over

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6 The line $y + 2x = 12$ intersects the curve $y = 2x^2 - 6x - 4$ at two distinct points A and B.

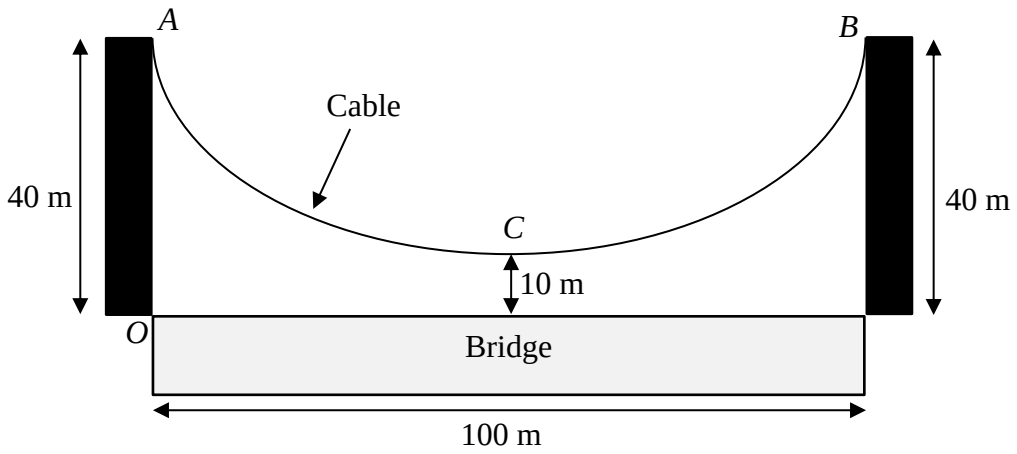
(i) Find the coordinates of A and of B. [3]

(ii) Hence, find the equation of the perpendicular bisector of AB. [4]

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7 **(a)** Find the range of values of x that satisfy the inequality $5x-3<2x(5-x)$. [3]

(b)



The diagram shows a horizontal bridge of 100 metres supported by 2 pillars at the side, with a cable being suspended from point A and B. Each pillar is vertical and is 40 metres tall. The lowest point C of the cable is 10 meters above the bridge. The origin, O, is vertically below point A, where the foot of the pillar meets the bridge.
A quadratic function can be used to model the cable. Find the quadratic equation. [3]

[Turn Over

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8 The function $f(x)$, a polynomial of degree four, has stationary points at $A(1, 5)$ and $B(4, 0)$.
$f(x)$ is an increasing function when $x > 4$.
$f(x)$ is **not an increasing** function when $x < 4$.

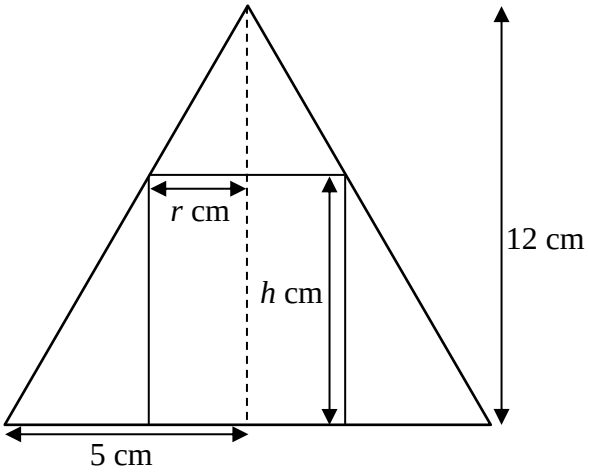
(i) State the nature of the stationary points A and B. Explain your answer. [4]

(ii) Given that $f'(x) = a(x-1)^2(x-4)$, where a is a non-zero constant, find an expression for $f(x)$. [5]

[Turn Over

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9



A cone of height 12 cm and base radius 5 cm is placed over a cylinder of radius r cm and height h cm. The cone is in contact with the cylinder along the cylinder's upper rim. The diagram shows a vertical cross-section of the cone and the cylinder.

(i) Express h in terms of r. [2]

(ii) Hence show that the volume, V cm^3, of the cylinder is given by

$$V = 12\pi r^2 - \frac{12}{5}\pi r^3 .$$ [1]

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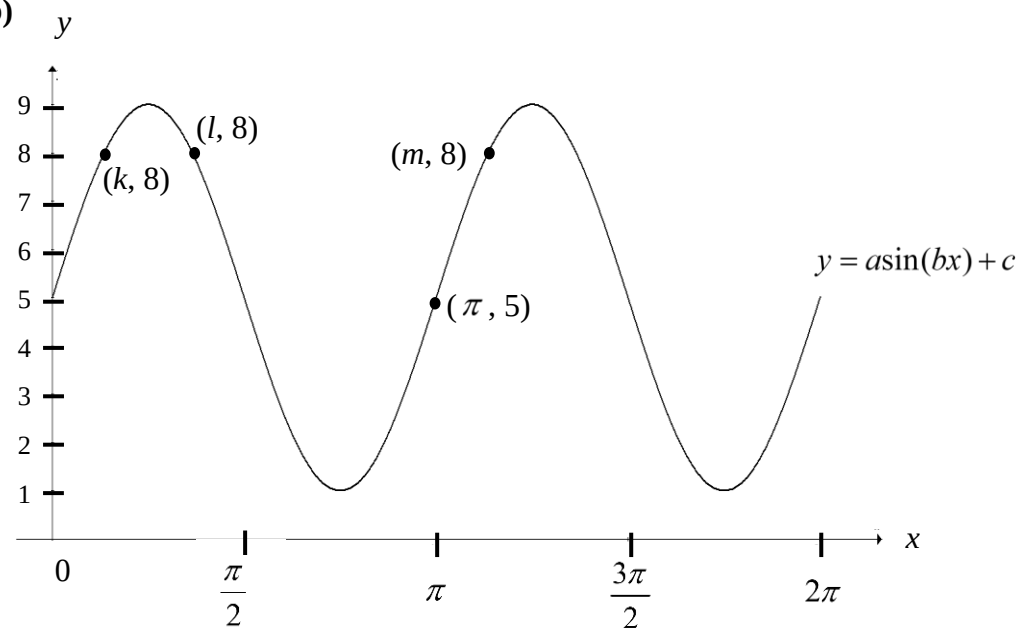
(iii) Calculate the maximum value of V. [5]

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10 **(a)** Calculate, in degrees, the **principal values** of x which satisfy $2\sin 2x + 3\cos x = 0$. [3]

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10 (b)



The diagram above shows part of the graph of $y = a\sin(bx) + c$, passing through points $(\pi, 5)$, $(k, 8)$, $(l, 8)$ and $(m, 8)$, where a, b, c, k, l and m are constants.

(i) Write down the values of a, of b and of c. [3]

Using the symmetry of the graph, or otherwise, find an equation connecting

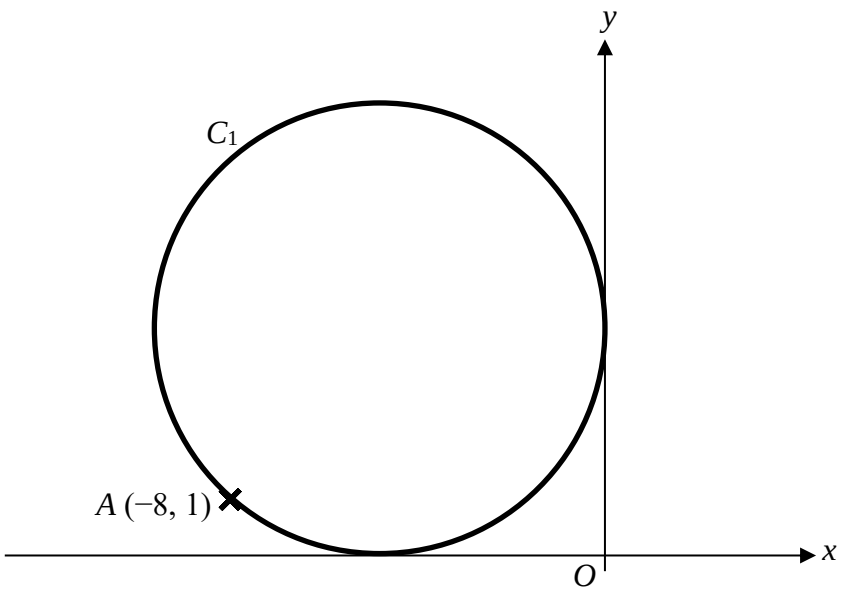
(ii) π, k and m, [1]

(iii) π, k and l. [1]

[Turn Over

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11 (a)



The negative x-axis and the positive y-axis are tangents to the circle C_1 with radius r. $A(-8, 1)$ lies on C_1.

(i) What can be deduced about the coordinates of the centre of C_1? [1]

(ii) Find the equation of C_1. [5]

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11 (b) Another circle, C_2 has equation $x^2 + y^2 - 14x - 20y = -113$.
Let P be the centre of C_2.

(i) State the coordinates of P and calculate the radius of C_2. [3]

S is a point outside C_2. Q and R are two distinct points on C_2.

(ii) Explain the relationship of SQ and SR if angle QSR is maximum. [2]

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12 A particle travelling in a straight line passes through a fixed point O with a velocity of 3 m/s. The acceleration, a m/s^2, of the particle, t seconds after passing through O, is given by $a = -e^{-0.3t}$. The particle comes to instantaneous rest at the point P.

(i) Show that the particle reaches P when $t = \frac{10}{3}\ln 10$. [6]

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(ii) Calculate the distance OP. [4]

(iii) Explain why the particle is again at O at some instant during the thirty-fourth second. [2]

End of Paper

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